

FIBEROPTIC CURRENT SENSOR HAVING A PLURALITY OF SENSOR HEADS**DESCRIPTION****Technical Field**

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This non-provisional application claims priority under 35 U.S.C. §119(e) from Provisional Patent Application No. 60/447,294 filed on February 14, 2003, which is herein incorporated by reference.

10 The invention relates to the field of fiberoptic sensors. It relates to a fiberoptic sensor for measuring current or magnetic field in accordance with the preamble of patent claim 1, and to a method for measuring an electric current or magnetic field in
15 accordance with the preamble of patent claim 12.

Prior art

Such a current sensor is known, for example, from EP 1
20 154 278 A2. This sensor has a light source, a detector, a signal processor and in addition a modulator circuit and two sensor heads. Light is coupled from the light source into the modulator circuit and propagates from there into the two sensor heads. Such a sensor head
25 includes a magnetooptically active sensor fiber, which is arranged in the shape of a coil around an electric conductor in which the electric current to be measured flows. The Faraday effect thereby produces a differential phase shift between two mutually
30 orthogonally polarized lightwaves propagating in such a sensor head.

The sensor heads in each case have a mirrored end such that, together with the remainder of the optical
35 structure, they each form a reflection interferometer. After the reflection at the mirrored ends, the light is guided back through the modulator circuit and coupled into the detector. The signal processor evaluates the

signals of the detector. The modulator circuit has an end on the side of the light source and detector, and an end on the side of the sensor head. It serves the purpose of the non-reciprocal modulation of a differential phase of two lightwaves that propagate in opposite directions and are polarized parallel to one another. For this purpose, the modulator circuit includes a piezoelectric phase modulator that is operated with its resonant frequency and is controlled by the signal processor.

The non-reciprocal differential phase modulation achieved by means of the modulator circuit serves the purpose of achieving a higher resolution in the detection of the differential phase shift induced by the Faraday effect. The effective operating point of the interferometer is shifted in a linear region of the cosinusoidal interference function.

A time division multiplexing method is used in order to be able to distinguish in the signal processor between the signals originating from the two different sensor heads. The light source is operated in a pulsed fashion, and the lengths of the two reflection interferometers are selected to be of different magnitudes. This produces transit times of different length for signals (or lightwaves) that originate from the various sensor heads, and so these signals arrive at various times in the signal processor and can thereby be distinguished.

A disadvantage of this type of sensor is that the achievable signal-to-noise ratio is not optimum, because a signal is not generated continuously at the detector, but only during a fraction of the measuring time, because of the pulsed operation. A further disadvantage is that owing to the different lengths of the two reflection interferometers, the amplitude with

which the phase modulator is operated can be optimally selected only for one of the two sensor fibers.

Another current sensor is known from G. Frosio,
5 R. Dändliker, "Reciprocal Reflection Interferometer for
a Fiber-Optic Faraday Current Sensor", *Appl. Opt.* 33,
6111 (1994). This likewise has a reflection geometry,
but includes only one sensor head. In order to produce
a non-reciprocal differential phase modulation, this
10 sensor likewise has a piezoelectric phase modulator.
The latter is not arranged in a modulator circuit. It
modulates the differential phase of two mutually
orthogonally polarized lightwaves propagating in the
same direction. Substantially larger driver voltages
15 are required at the piezomaterial of the modulator,
since a direct modulation of the birefringence of the
fiber of the modulator must be produced.

J. Blake, P. Tantaswadi, and R.T. de Carvalho disclose
20 in figure 1 of the publication "In-line Sagnac
Interferometer Current Sensor", *IEEE Transactions on
Power Delivery*, 11, 116-121 (1996) a further current
sensor. This sensor has a Sagnac geometry and includes
only one sensor head. Like the sensor described by
25 Frosio and Dändliker, it is also necessary here for a
large driver voltage to be present at the piezomaterial
of the modulator, since the differential phase of two
mutually orthogonally polarized lightwaves propagating
in the same direction is modulated by means of direct
30 modulation of the birefringence.

Summary of the invention

It is an object of the present invention to create a
35 current sensor of the type mentioned at the beginning,
and a corresponding measurement method, it be aimed not
to give rise to the above named disadvantages. The aim,

in particular, is for the sensor to have an improved signal-to-noise ratio.

This object is achieved by a fiberoptic current sensor
5 having the features of patent claim 1, and a corresponding measurement method in accordance with patent claim 12.

The fiberoptic sensor according to the invention for
10 measuring at least one electric current or magnetic field has: a light source; N sensor heads that can be arranged in the shape of a coil around current conductors or along the magnetic field, N being a whole number with $N \geq 2$; at least one phase modulation unit
15 having at least one phase modulator; at least one detector; and a control and evaluation unit that is connected via at least one detector signal line to the at least one detector, and via at least one modulator signal line to the at least one phase modulator. In
20 this case, first means are available for guiding light from the light source into an end, on the detector side, of the phase modulation unit, and second means are available for guiding light from the end, on the detector side, of the phase modulation unit to the
25 detector, and the at least one phase modulation unit has one further end, on the sensor head side, which is optically connected to at least one of the sensor heads, and linearly polarized lightwaves can be phase-modulated differentially in a non-reciprocal fashion by
30 means of the at least one phase modulation unit.

The sensor is distinguished by virtue of the fact that N modulation amplitudes $\phi_{0,n}$ and N modulation frequencies ν_n are provided for the non-reciprocal
35 differential phase modulations, the modulation frequencies ν_n and two prescribable positive whole numbers p, q with $p \neq q$ being selected in such a way

that it holds for all positive whole numbers z and for all whole numbers n, m with $n \neq m$ and $1 \leq n, m \leq N$ that:

$$\begin{aligned} p \cdot v_n &\neq z \cdot v_m \text{ and} \\ q \cdot v_n &\neq z \cdot v_m, \end{aligned}$$

and the modulation amplitudes $\phi_{0,n}$ and the modulation frequencies v_n being selected as a function of modulation-relevant optical path lengths ℓ_n .

Thus, N different modulation frequencies v_n are used for the non-reciprocal modulation of the differential phase of the lightwaves in the case of a sensor comprising N sensor heads. These modulation frequencies v_n and two positive whole numbers p and q are selected in such a way that a p -fold and a q -fold multiple of each of the modulation frequencies v_n differs from all the harmonics of each of the other modulation frequencies v_n . Moreover, the modulation amplitudes $\phi_{0,n}$ and the modulation frequencies v_n are selected as a function of modulation-relevant optical path lengths ℓ_n . These modulation-relevant optical path lengths ℓ_n are essentially the optical path lengths which lightwaves traverse from the at least one phase modulator through the n^{th} sensor head and back to the same at least one phase modulator. Corrections that are to be added to this optical path length, for example in the case of modulator circuits with fiber branches of different length as phase modulation units, are specified further below in the description.

It is advantageous that on the basis of such a design it is possible, on the one hand, for the signals that originate from various sensor heads to be uniquely assigned via their frequency to the appropriate sensor head on the basis of the conditions for the modulation frequencies v_n . On the other hand, the modulation amplitudes $\phi_{0,n}$ and the modulation frequencies v_n can be

selected in such a way that it is possible to set an optimum detectability and an optimum signal-to-noise ratio for each of the N sensor heads.

5 It is advantageous to select $p = 1$ and $q = 2$ such that signals of the first and second harmonics are detected and evaluated. The detected signals are particularly large thereby, and so the signal-to-noise ratio is optimum.

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In an advantageous embodiment of the invention, the sensor has exactly one control and evaluation unit. Signals that originate from the various sensor heads and are fed to the control and evaluation unit via the
15 at least one detector signal line are distinguished from one another in said unit by means of frequency filtering. These signals are converted in the control and evaluation unit into N output signals S_n that are a measure of the at least one current to be measured or
20 of the at least one magnetic field to be measured. In particular, the output signals S_n for each n with $1 \leq n \leq N$ are determined from signals at the frequencies $p \cdot v_n$ and $q \cdot v_n$ in the control and evaluation unit. The detection can take place in an open-loop or in a
25 closed-loop method. It is possible on the basis of the assignment of the signals to the sensor heads in terms of frequency to use a single control and evaluation unit to evaluate signals from all sensor heads, the result being to implement a very cost effective and
30 simple sensor.

A further advantageous embodiment of the invention is characterized in that it contains exactly one phase modulation unit. A very cost effective and simple
35 design is thereby implemented. The sensor has N reflection interferometers, each of the N reflection interferometers including exactly one of the N sensor heads, and the N sensor heads in each case having a

mirrored end. Such a sensor is insensitive to disturbances such as vibrations and is easy to produce. Moreover, it is possible to provide inherent temperature compensation such as is known from the prior art. The light source of such a sensor is advantageously operated in a pulsed fashion, and the detection is performed by means of a time division multiplexing method. The sensor therefore manages with a minimum of requisite components.

In the case of such a sensor, the phase modulation unit is advantageously either a modulator circuit having N phase modulators that are operated in each case with one of the N modulation frequencies v_n , or the phase modulation unit is a single phase modulator that permits a simultaneous phase modulation with the N various modulation frequencies v_n , that is to say is operated with a frequency spectrum of the N modulation frequencies v_n .

Another advantageous embodiment of the invention has N phase modulation units having one phase modulator each, the n th phase modulation unit being optically connected to the n th sensor head, and the n th phase modulator being operated with the modulation frequency v_n . Such a sensor can be operated without a time division multiplexing method, and so the light source can be operated continuously (in continuous wave mode). This results in an improved signal-to-noise ratio.

Such a sensor is advantageously designed in such a way that N reflection interferometers are provided, each of the N reflection interferometers including exactly one of the N sensor heads, and the N sensor heads in each case having a mirrored end, and that either the phase modulation units are modulator circuits, the differential phase of oppositely directed lightwaves polarized parallel to one another being modulated by

the phase modulators, or that the differential phase of lightwaves propagating in the same direction and mutually orthogonally polarized is modulated by each of the phase modulators, for example by means of
5 integrated optical modulators.

A corresponding sensor can also be designed with a Sagnac configuration.

10 An advantageous sensor according to the invention is advantageously operated with $p = 1$ and $q = 2$; the N modulation amplitudes $\phi_{0,n}$ and the N modulation frequencies ν_n being selected in such a way that
15 amplitudes $\alpha_{0,n}$ of the modulation of the differential phase of the linearly polarized lightwaves lie between 1.7 and 2.0, in particular between 1.8 and 1.88, or are essentially 1.84 for all n with $1 \leq n \leq N$. This results in maximum signals and an optimum signal-to-noise ratio.

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In the method according to the invention for measuring at least one electric current or at least one magnetic field, a light source emits lightwaves that are converted into linearly polarized lightwaves. The
25 linearly polarized lightwaves are guided into N sensor heads in which the lightwaves undergo a phase shift dependent on the current or magnetic field to be measured, N being a whole number with $N \geq 2$. The lightwaves undergo a non-reciprocal differential phase
30 modulation in at least one phase modulation unit with at least one phase modulator, and are detected in at least one detector. The at least one phase modulation unit is traversed by the lightwaves both during their propagation from the light source to the sensor heads,
35 and during their propagation from the sensor heads to the at least one detector. A control and evaluation unit is used, on the one hand, to control the at least one phase modulator and, on the other hand, also to

evaluate signals originating from the at least one detector.

The method is characterized in that the lightwaves are
5 differentially phase-modulated in a non-reciprocal
fashion with N modulation amplitudes $\phi_{0,n}$ and N
modulation frequencies ν_n . In this case, the modulation
frequencies ν_n and two prescribable positive whole
10 numbers p, q with $p \neq q$ are selected in such a way that
it holds for all positive whole numbers z and for all
whole numbers n, m with $n \neq m$ and $1 \leq n, m \leq N$ that:

$$p \cdot \nu_n \neq z \cdot \nu_m \text{ and} \\ q \cdot \nu_n \neq z \cdot \nu_m.$$

15

The modulation amplitudes $\phi_{0,n}$ and the modulation
frequencies ν_n are advantageously selected as a function
of modulation-relevant optical path lengths ℓ_n .

20 Signals of the p th and q th harmonics of the
 N modulation frequencies ν_n are detected, preferably by
means of frequency filtering. The modulation
frequencies ν_n are selected in such a way that these p th
and the q th harmonics are different from other signal
25 frequencies occurring, in particular from the other
harmonics of the modulation frequencies ν_n . This permits
the signals to be uniquely assigned via their frequency
to the corresponding sensor head. Moreover, the
selection of the various modulation frequencies ν_n for
30 the various sensor heads, together with a corresponding
selection of the modulation amplitudes $\phi_{0,n}$ of the non-
reciprocal differential phase shifts as a function of
modulation-relevant optical path lengths ℓ_n permits
optimum tuning of these values for each of the sensor
35 heads such that it is possible to set an optimum
detectability and an optimum signal-to-noise ratio.

Further preferred embodiments and advantages follow from the dependent patent claims and the figures.

Brief description of the drawings

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The subject matter of the invention is explained in more detail below with the aid of preferred exemplary embodiments that are illustrated in the attached drawings, in which:

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Figure 1 shows schematically a sensor in reflex configuration, having a modulator circuit, three phase modulators and three sensor heads;

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Figure 2 shows an illustration of the time profile of signals in the case of the time division multiplexing method;

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Figure 3 shows schematically a sensor in reflex configuration, having an integrated optical modulator and three sensor heads;

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Figure 4 shows schematically a sensor in reflex configuration, having three integrated optical modulators and three sensor heads;

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Figure 5 shows schematically a sensor in reflex configuration, having three modulator circuits with in each case one phase modulator, and having three sensor heads;

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Figure 6 shows schematically a sensor in Sagnac configuration, having three piezoelectric phase modulators and three sensor heads; and

Figure 7 shows schematically a sensor in reflex configuration, having three modulator

circuits with in each case one phase modulator, having three sensor heads and having three detectors.

5 The reference symbols used in the drawings, and their meaning, are listed in summary in the list of reference symbols. Identical, or at least identically acting parts are basically provided in the figures with identical reference symbols. The exemplary embodiments
10 described represent the subject matter of the invention by way of example and are not restrictive.

Ways of implementing the invention

15 A few details known from the prior art and relating to the design of similar sensors and to the generation of non-reciprocal differential phase modulations are not illustrated below and can be taken from the abovementioned EP 1 154 278 A2, which is therefore
20 hereby incorporated into the description together with its entire disclosure content.

An embodiment of the invention is illustrated in figure 1. A superluminescence diode 1 serving as low
25 coherence light source 1 emits lightwaves in a first means 6 for guiding light of the light source 1 into an end 3, on the detector side, of a phase modulation unit PME. This first means 6 essentially comprises a fiber coupler 14 and, if appropriate, additionally one or two
30 further fiber pieces by means of which the light source 1 and the phase modulation unit PME are optically connected to opposite sides of the fiber coupler 14.

The light source 1 is advantageously a low coherence
35 light source, for example a luminescence diode, a superluminescence diode or a laser diode operated below the laser threshold. The coherent lengths are then typically of the order of magnitude of 50 μm . Another

possible light source 1 is a broadband fiber source, for example an erbium-doped fiber that can advantageously be pumped by a semiconductor laser with an emission wavelength of 980 nm or 1480 nm for example.

Serving as phase modulation unit PME in figure 1 is a modulator circuit PME. The latter has an end 3 on the detector side, and an end 4 on the sensor head side. These two ends 3, 4 are formed by fiber couplers 3, 4. The modulator circuit PME has two fiber branches between the two ends 3, 4. A polarizer 8 or 8', respectively, is arranged in each of the two fiber branches. A 90° splice 9 is arranged as means for changing the direction of polarization 9 in one of the fiber branches. N = 3 piezoelectric phase modulators PM₁, PM₂, PM₃ are arranged one behind another in the other fiber branch. N is the number of the sensor heads H₁, H₂, H₃ of the sensor. The first sensor head H₁ is provided at an output of the coupler 4 on the sensor head side. Provided at the other output of the coupler 4 on the sensor head side is a fiber coupler 15 to whose two outputs the further two sensor heads H₂, H₃ are connected.

The three sensor heads H₁, H₂, H₃ are of similar design. They have one optional fiberoptic supply lead 10₁, 10₂, 10₃, each, one phase delay element 11₁, 11₂, 11₃ each, and one sensor coil 12₁, 12₂, 12₃ each. For the sake of clarity, 10_n, 11_n etc are described below. For the sake of clarity, some reference symbols that follow from the remainder of the figure or in conjunction with the other figures are not used in the figures. The phase delay element 11_n is a $\lambda/4$ element that generates a 90° phase delay, or else another phase delay, typically lying near 90°. It connects the fiberoptic supply lead 10_n to one end of the sensor coil 12_n. The sensor coil 12_n comprises a magnetooptically active

fiber 12_n , preferably having a round core cross section. The other end 13_n of the sensor coil 12_n is mirrored, or has a mirror 13_n . Each sensor head H_n is arranged in the shape of a coil around a current
5 conductor C_n in which an electric current $I_{el,n}$ to be measured flows.

After a reflection at a mirrored end 13_n , the lightwaves return again. Starting from the end 3, on
10 the detector side, of the phase modulation unit PME, the light is guided from the end 3, on the detector side, of the phase modulation unit PME to a detector 2 via a second means 7 for guiding light.

15 The detector 2 is a photodetector, for example a photodiode or photomultiplier.

The sensor also has a control and evaluation unit 5 that includes a signal processor. The control and
20 evaluation unit 5 is connected to the detector 2 via a detector signal line D, and to each of the three phase modulators PM_n via three modulator signal lines M_n . Moreover, the control and evaluation unit 5 is also connected to the light source 1 via a light control
25 signal line L. The control and evaluation unit 5 evaluates the signals, originating from the detector 2, in output signals S_n that are a measure of the magnitude of the electric currents $I_{el,n}$ or magnetic fields to be measured.

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The optical elements arranged between the polarizers 8, 8' and the phase delay elements 11_n are polarization maintaining. These are advantageously optical fibers having an elliptic core cross section. The optical
35 elements arranged between the polarizers 8, 8' and the light source 1 and the detector 2, respectively, are advantageously also polarization maintaining. This also holds for the other embodiments of the invention.

The light emitted by the light source 1 is split between the two fiber branches of the modulator circuit at the coupler 3, preferably in the ratio of intensity 1:1. The light is linearly polarized in the polarizers 8,8'. Mutually orthogonally polarized lightwaves then pass into the coupler 4 because of the 90° splice 9. In the 90° phase delay element 11_n, the mutually orthogonally polarized lightwaves are converted into left and right circularly polarized lightwaves. Because of the magnetic field of the current to be measured, said lightwaves undergo phase shifts of different magnitude in the sensor coil 12_n. After reflection at the mirrored end 13_n, the circularly polarized lightwaves are reconverted into mutually orthogonally polarized lightwaves during the second traverse of the 90° phase delay element 11_n. Because of the non-reciprocal Faraday effect, these converted lightwaves have a differential phase shift of

$$\Delta\phi_n = 4 \cdot V_n \cdot R_n \cdot I_{el,n}.$$

Here, V_n is the Verdet constant of the material of a sensor coil 12_n (for example $2.65 \cdot 10^{-3}$ Rad/A at 820 nm light wavelength); R_n is the number of turns of the sensor coil about a current conductor; $I_{el,n}$ is the current to be measured, which flows in the current conductor C_n . The fact that the phase shift is non-reciprocal means that it accumulates and is not cancelled by the twofold traverse of the sensor coil 12_n (once in the opposite direction in each case).

Elliptically polarized light instead of circularly polarized light results when the phase delay elements 11_n do not produce a phase shift of exactly 90°. This results in corresponding corrections by comparison with the specified equation for $\Delta\phi_n$, and these are known from the prior art.

The non-reciprocally phase shifted, mutually orthogonally polarized lightwaves traverse the phase modulation unit PME. The light is transmitted from the end 3, on the detector side, of the phase modulation unit PME to the detector 2 via the second means 7 for guiding light. The second means 7 is partially identical to the first means 6. It comprises the coupler 14 and, if appropriate, one or two further fiber pieces. A photodiode 2 serves as detector 2. The non-reciprocal phase shift $\Delta\phi$ induced by the Faraday effect is a measure of the magnitude of the electric current to be measured.

The modulator circuit PME serves for the non-reciprocal modulation of a differential phase of two lightwaves propagating in opposite directions and polarized parallel to one another. The effective operating point of the interferometer is thereby displaced in a linear region of the cosinusoidal interference function. A greater resolution in the detection of the differential phase shift $\Delta\phi$ induced by the Faraday effect is achieved in this way.

The modulator circuit PME includes three preferably piezoelectric phase modulators PM_1, PM_2, PM_3 in accordance with the number N of sensor heads H_n . A piezoelectric phase modulator essentially comprises a piece of piezoelectric material and a piece of optical fiber that is wound around the piezoelectric material. Each of the phase modulators PM_n is advantageously operated at its resonant frequency. Owing to the operation at the resonant frequency, relatively low driver voltages can already suffice to generate a large phase modulation amplitude $\phi_{0,n}$ for the individual lightwaves. The amplitudes of the differential phase shift between the two lightwaves propagating in opposite directions and polarized parallel to one another may be taken as $\alpha_{0,n}$. The frequencies of the modulations may be taken as

v_n . The signal at the photodiode 2 is then modulated with the modulation frequencies v_n and their harmonics.

The first step is to consider the case in which modulation is performed with the aid of a phase modulator PM_n and a single modulation frequency v_n , and there is one sensor head H_n , that is to say $N = 1$ and $n = 1$:

For Faraday phase shifts $\Delta\phi_n < 90^\circ$, $\Delta\phi_n$ can be determined from the amplitudes $I_{Det,vn} = I_0 \cdot J_1(\alpha_{0,n}) \cdot \sin\Delta\phi_n$ of the photodiode signals of the first harmonic v_n and, respectively, $I_{Det,2vn} = I_0 \cdot J_2(\alpha_{0,n}) \cdot \cos\Delta\phi_n$ of the second harmonic $2 \cdot v_n$ in accordance with

$$\Delta\phi_n = \arctan \{ [I_{Det,vn} / I_{Det,2vn}] \cdot [J_2(\alpha_{0,n}) / J_1(\alpha_{0,n})] \},$$

 I_0 being constant, in general unknown light amplitudes, and J_1 and J_2 being the Bessel functions of first and second order, respectively.

It holds approximately for small Faraday phase shifts $\Delta\phi_n$ with $\Delta\phi_n \ll 1$ (in radians) that

$$\Delta\phi_n = [I_{Det,vn} / I_{Det,2vn}] \cdot [J_2(\alpha_{0,n}) / J_1(\alpha_{0,n})].$$

The type of signal detection and evaluation described is a so-called open-loop detection. Closed-loop detection exists as an alternative to the open-loop detection. In the closed-loop detection, $\Delta\phi_n$ is compensated at the phase modulator PM_n by applying an appropriate control signal. For this purpose, an amplitude of the photodiode signal is controlled to zero, preferably at the first harmonic, that is to say at $I_{Det,vn}$. The magnitude of the control signal is a measure of $\Delta\phi_n$ and of the current $I_{el,n}$ to be measured.

The modulation amplitudes $\alpha_{0,n}$ of the differential phases are given by

$$\alpha_{0,n} = 2 \cdot \phi_{0,n} \cdot \sin(2\pi v_n T_n / 2),$$

T_n being the modulation-relevant circulation time of the light. T_n is given as $T_n = \ell_n / c$ with the modulation-relevant optical path length ℓ_n and the speed of light vacuum c . The optical path length is the product of the
5 geometric path length and the effective refractive index. When the optical design is configured in such a way that a lightwave is modulated in the n th phase modulator PM_n both before traversing the n th sensor head H_n and after traversing the n th sensor head H_n , T_n
10 is the time required by a lightwave when it runs from the n th modulator PM_n as far as through the n th sensor head H_n and back again to the n th modulator PM_n . ℓ_n is the corresponding optical path length. In the case of a reflective design having a modulator circuit PME_n that
15 includes a phase modulator PM_n and whose fiber branches both have the same optical length, the modulation-relevant circulation time T_n is twice the time required by a lightwave when it runs from the phase modulator PM_n as far as the mirror 13_n of the sensor head H_n (a
20 wave that was phase-modulated on the outward path runs on the return path through the fiber branch of the phase modulation unit that does not include the phase modulator). Correspondingly ℓ_n is then twice the optical path length from the phase modulator PM_n up to
25 the mirror 13_n of the sensor head H_n . In the case where the modulator circuit PME_n has two fiber branches of different length, in order to maintain ℓ_n it is necessary further to add to this optical path length that optical difference path length by which the second
30 fiber branch is longer than the first fiber branch, which includes the phase modulator PM_n . This difference path length to be added on is negative when the second fiber branch is shorter than that containing the phase modulator PM_n . The modulation-relevant circulation time
35 T_n behaves correspondingly in the case of fiber branches of different length: a further (positive or negative) difference time must be added on for the said difference path length at twice the time required by a

lightwave from the phase modulator PM_n up to the mirror 13_n of the sensor head H_n .

5 For a given driver voltage of a phase modulator PM_n and an amplitude $\phi_{0,n}$, resulting therefrom, of the phase modulation, in accordance with the above equation $\alpha_{0,n}$ is a maximum for

$$\ell_n = (2p-1) \cdot c / (2v_n), \quad \text{with } p = 1, 2, 3, \dots$$

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By contrast, $\alpha_{0,n}$ vanishes for

$$\ell_n = p \cdot c / (2v_n), \quad \text{with } p = 1, 2, 3, \dots$$

15 The modulation amplitudes $\phi_{0,n}$ and the modulation frequencies v_n are selected for all n as a function of the respective optical path length ℓ_n . In this case, the modulation frequencies v_n are mostly advantageously prescribed by being selected (in the case of
20 piezoelectric phase modulators) as resonant frequency of the corresponding phase modulator PM_n .

The following may now be said concerning the case of $N \geq 2$, that is to say a plurality of sensor heads and a
25 plurality of modulation frequencies:

A further boundary condition is added for $N \geq 2$, specifically that lightwaves which have traversed the n th sensor head H_n are incoherent at the detector 2
30 with lightwaves that have traversed the m th sensor head H_m , for $n \neq m$. The corresponding lightwaves are thereby not capable of interference, and so disturbing superpositions and reciprocal influences are avoided. This condition is achieved by appropriate selection of
35 the total optical circulation lengths Λ_n covered by lightwaves from the light source 1 through the n th sensor head H_n to the detector 2 (or 2_n).

Furthermore, the generally substantially stricter condition that the term $(\Lambda_n - \Lambda_m) \cdot \Delta n_{gr}$ is substantially greater than the coherent length of the light source 1 for $n \neq m$ is also advantageously satisfied. In this case, Δn_{gr} is the difference between the group refraction indices for the two mutually orthogonal light modes. Satisfying this condition prevents lightwaves that have been produced by undesired mode coupling from leading to disturbing interference signals.

Signals arrive at the detector 2 that are modulated by the n th phase modulator PM_n and come from the m th sensor head H_m ; $1 \leq n, m \leq N$. In the case of the first harmonic (v_n), such signals I_{Det, m, v_n} , and in the case of the second harmonic ($2v_n$) such signals $I_{Det, m, 2v_n}$, are given by

$$\begin{aligned} I_{Det, m, v_n} &= J_1(\alpha_{0, n}) \cdot \sin \Delta \phi_m \cdot \sin(2\pi v_n t) \\ I_{Det, m, 2v_n} &= J_2(\alpha_{0, n}) \cdot \cos \Delta \phi_m \cdot \sin(4\pi v_n t). \end{aligned}$$

The driver voltages of the phase modulators PM_n , and thus the phase modulation amplitudes $\phi_{0, n}$ are selected in conjunction with the corresponding modulation frequencies v_n as a function of the optical path lengths ℓ_m . In particular, $\phi_{0, n}$ and v_n are preferably selected in such a way that for $n = m$ each of the amplitudes $\alpha_{0, n}$ of the modulation of the differential phase has the value $\alpha_{0, n} = 1.84$. The first maximum of the first Bessel function J_1 lies at the value 1.84 (in radians). It is possible in this way to achieve an optimum signal-to-noise ratio, specifically for the signals of each of the sensor heads H_m . Depending on the optical path lengths, $\alpha_{0, n}$ is generally different from the optimum value (1.84) for $n \neq m$.

The signals I_{Det, m, v_n} and $I_{Det, m, 2v_n}$ at the frequencies v_n and $2 \cdot v_n$, respectively, can be separated from one

another in the control and evaluation unit 5 by means of frequency filtering. For this purpose, the modulation frequencies v_n are selected in such a way that

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$$v_i \neq v_j \text{ and } 2 \cdot v_i \neq v_j$$

holds, i, j being whole numbers with $i \neq j$ and $1 \leq i, j \leq N$, N denoting the number of sensor heads H_n of the sensor, which are selected as $N = 3$ in the
10 exemplary embodiment of figure 1.

It is also possible in principle when determining the Faraday phase shift $\Delta\phi_n$ to operate with other harmonics, for example with the third and fourth ones, as an
15 alternative or in addition to the first and the second harmonics in order to determine the current to be measured. The conditions for the selection of the modulation frequencies v_n are then to be adapted correspondingly such that none of the harmonics used
20 coincide with another frequency or harmonics thereof. By analogy with the above equation, it then therefore holds for all positive whole numbers z that

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$$p \cdot v_i \neq z \cdot v_j \text{ and } q \cdot v_i \neq z \cdot v_j,$$

i, j being whole numbers with $i \neq j$ and $1 \leq i, j \leq N$ and p and q being positive whole numbers different from one another. Detection is then performed for the p th and
30 q th harmonics of the modulation frequencies v_n .

Since in a design in accordance with figure 1 each lightwave that originates from one of the three sensor heads H_n is modulated with all three phase modulators
35 PM_n , it is required to be able to separate these signals from one another in the control and evaluation unit 5, and to assign them to the respective currents to be measured. Use is made for this purpose of a time

division multiplexing method by means of which the signals from the various sensor heads H_n can be discriminated temporarily.

5 Figure 2 illustrates the temporal profile of the signals schematically for the exemplary embodiment of figure 1. The horizontal axis is the time axis t . The vertical axis illustrates light intensities at the detector 2 (continuous lines) and at the light source 1 (dashed lines). The light source 1 is operated in pulsed fashion with a pulse duration τ and a pulse spacing Δt . The control of the light source is performed via the light control signal line L by means of the control and evaluation unit 5. The total optical circulation lengths Λ_n that lightwaves cover from the light source 1 through the n th sensor head H_n to the detector 2 are selected in such a way that pulses which traverse various sensor heads are temporarily separated at the photodiode 2. The total circulation lengths Λ_n must differ for this purpose from one another by more than $c \cdot \tau$. For a pulse duration of, for example, $\tau = 1 \mu s$, the path length differences (outgoing and returning together) must be greater than approximately 200 m, and be 300 m, for example. The optical path length for the nearest coil, that is to say the smallest Λ_n , can be smaller than $c \cdot \tau$, however. The interfering optical signals from individual sensor heads H_n then reach the photodiode 2 in corresponding time windows, that is to say spaced apart in time. In the case of N sensor heads, exactly N pulses are recorded with time delays $\Delta \tau_n$, $n = 1, 2, \dots, N$ ($\Delta \tau_n$ being measured from the generation of the light pulse in the light source 1) per light pulse emitted by the light source 1. Each light pulse arriving at the detector includes signals that are modulated with all the modulation frequencies ν_n and their harmonics.

Figure 2 illustrates the case in which the segments are staggered in accordance with $\Lambda_n = n \cdot \Lambda_1$. The path length difference between the n th total circulation lengths Λ_n and the $(n+1)$ th path length Λ_{n+1} is thus exactly Λ_1 . For $\Lambda_1 = 300$ m, the time delays of the pulses at the detector 2 are then $\Delta\tau_n = n \cdot 1.5 \mu\text{s}$. The temporal spacing Δt of the emitted pulse (pulse spacing Δt) must in this case be at least $\Delta t \geq \tau_N = N \cdot \tau_1$, corresponding to $4.5 \mu\text{s}$ in the example mentioned and illustrated. It is clear that a pulse duration τ that is substantially longer than $1 \mu\text{s}$ entails the disadvantage of very long fiber segments. The path length differences $\Lambda_{n+1} - \Lambda_n$ must additionally satisfy the condition of being longer than the coherent length of the light of the light source 1.

Typical modulation frequencies ν_n as resonant frequencies of piezoelectric crystals are of the order of magnitude of 10 kHz to several 100 kHz. Consequently, a typical pulse duration τ of a laser pulse of approximately $1 \mu\text{s}$ is substantially shorter than the period $1/\nu_n$ and $1/(2\nu_n)$ of the signals $|_{\text{Det},m,\nu_n}$ and $|_{\text{Det},m,2\nu_n}$. In order to sample one or more periods of the signals $|_{\text{Det},m,\nu_n}$ and $|_{\text{Det},m,2\nu_n}$, there is consequently a need for a correspondingly large number of pulses, and the repetition frequency of the pulses $1/\Delta t$ must differ from ν_n and $2\nu_n$.

Relatively high modulation frequencies ν_n in the range from 1 MHz to over 10 MHz can be achieved with integrated optical modulators PM_n , for example on lithium niobate substrates, or with the aid of fiber segments that are provided with a piezoelectric coating. One or more periods of the signals $|_{\text{Det},m,\nu_n}$ and $|_{\text{Det},m,2\nu_n}$, can then be sampled within a light pulse.

A further advantageous embodiment of the invention is illustrated in figure 3. It corresponds largely to the

embodiment illustrated in figure 1, and will be described starting therefrom. In essence, here the modulator circuit PME is replaced by a phase modulation unit PME that includes an integrated optical modulator PM as phase modulator PM. The phase modulation unit PME further includes a (single) fiber polarizer 8 that is optically connected to the coupler 14, and a 45° splice 9' arranged between the polarizer 8 and the integrated optical modulator PM. The fiber polarizer 8 serves for linearly polarizing the lightwaves. The 45° splice 9' generates mutually orthogonally polarized lightwaves. The end 4, on the sensor head side, of the phase modulation unit PME is preferably formed by an (asymmetric) 1x2 fiber coupler 16.

Although not illustrated in figure 3, it is possible as an alternative for the integrated optical phase modulator PM to be designed in such a way that it not only generates the phase modulation, but also takes over the function of the fiber coupler 16, that is to say splits the lightwaves into two lightwave trains, one for the first sensor head H_1 , and one for the further two sensor heads H_2, H_3 .

The only one phase modulator PM requires only one modulator signal line M instead of three modulator signal lines M_n .

The control and evaluation unit 5 transmits to the integrated optical modulator PM a modulator signal that permits a simultaneous phase modulation with N different modulation frequencies ν_2 , $N = 3$ in figure 3. The modulator signal is then a frequency spectrum or a superposition of the N frequencies ν_n . The integrated optical phase modulator modulates the phases of mutually orthogonally polarized lightwaves that propagate in the same direction, doing so by direct modulation of the birefringence.

Since, as also in the exemplary embodiment of figure 1, only one phase modulation unit PME, by means of which lightwaves from all three sensor heads H_n are phase-modulated, is provided in the exemplary embodiment of figure 3, this sensor is also operated in a time division multiplex method, for example with the method described in conjunction with figures 1 and 2.

Figure 4 shows a further advantageous embodiment of the invention. Once again, this is a sensor having a light source 1, a detector 2, a control and evaluation unit 5 and $N = 3$ sensor heads H_n in reflex configuration. However, the sensor has $N = 3$ phase modulation units PME_n having one phase modulator PM_n each. The three sensor heads H_n are of similar design. Their design corresponds to that of the sensor heads described in conjunction with figure 1. Each of the three phase modulation units PME_n is of the same design as the phase modulation unit described in conjunction with figure 3. Thus, it is possible by means of each of the phase modulators PM_n to modulate the differential phase of mutually orthogonally polarized lightwaves propagating in the same direction. This is performed by means of a direct modulation of the birefringence. The phase modulators PM_n are advantageously designed as integrated optical phase modulators PM_n .

Light is guided into each of the three phase modulation units PME_n via first means 6 for guiding light of the light source 1 into the ends 3_n , on the detector side, of the phase modulation units PME_n . These first means 6 include two fiber couplers 14 and 17 and, if appropriate, further fiber pieces. The fiber couplers 14, 17 are advantageously designed in such a way that substantially the same light intensity is coupled into each of the phase modulation units PME_n . Each of the phase modulation units PME_n is optically connected at

its end 4_n on the sensor head side to one sensor head H_n in each case. Light returning from the sensor heads H_n is fed to the detector 2 via second means 7 for guiding light from the ends 4_n , on the detector side, of the
5 phase modulation units PME_n to the detector 2. These second means 7 include the two fiber couplers 14 and 17 and, if appropriate, further fiber pieces.

In a design in accordance with figure 4, the evaluation
10 has no need of a time division multiplexing method, because in the n th phase modulation unit PME_n it is only those lightwaves which have undergone a Faraday phase shift $\Delta\phi_n$ in the n th sensor head H_n that are phase modulated. The signal from the n th sensor head H_n is
15 modulated with the respective modulation frequency ν_n , and can therefore be uniquely assigned in the control and evaluation unit 5 by assigning the frequencies or by frequency filtering. The light source 1 can be
20 operated in the cw mode, that is to say continuously. A substantially improved signal-to-noise ratio is thereby achieved. A light control signal line L is not required in such a cw operated sensor.

As in the above exemplary embodiments, with a sensor in
25 accordance with figure 4 the total optical circulation lengths Λ_n are also selected in such a way that disturbing superpositions and reciprocal influences are avoided: The N total circulation lengths Λ_n therefore differ from one another by at least the coherence
30 length of the light source 1. Again, the condition is also advantageously satisfied that the term $(\Lambda_n - \Lambda_m) \cdot \Delta n_{gr}$ is substantially greater than the coherence length of the light source 1 for $n \neq m$.

35 Since one modulation frequency ν_n each can be selected per sensor head H_n , said frequency can be selected in each case such that an optimum amplitude $\alpha_{0,n}$ is

achieved for the modulation of the differential phase, and thus an optimum signal-to-noise ratio is achieved.

5 Sensors having integrated optical phase modulators are advantageously operated with closed-loop detection. The reciprocal of half the modulation frequency ν_n corresponds in this case to the modulation-relevant circulation time T_n of the light, and the Faraday phase shift $\Delta\phi_n$ is compensated at the modulator.

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Figure 5 shows a further embodiment, which is similar to the embodiment from figure 4 and is described starting therefrom. Instead of the phase modulation units PME_n having integrated optical phase modulators PM_n , modulator circuits PME_n having piezoelectric phase modulators PM_n are provided in figure 5 as phase modulation units PME_n . The modulator circuits PME_n are described in conjunction with figure 1 and in the abovementioned EP 1 154 278 A2. Each of the phase modulators PM_n modulates the differential phase of two lightwaves propagating in opposite directions to one another and polarized parallel to one another.

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Figure 6 shows a current sensor with $N = 3$ sensor heads H_n in Sagnac configuration. Thus, together with a part of the residual optical structure of the sensor, the three sensor heads H_n each form a Sagnac interferometer. The design is described starting from the design in figure 4. By contrast with figure 4, in figure 6 the three phase modulation units PME_n , the three sensor heads H_n and the means 6, 7 for guiding light are designed in a different way. The sensor heads H_n have two feeder fibers 10_n , $10_n'$ and no mirrored end. Each of the phase modulation units PME_n consist essentially of one phase modulator PM_n each, which can be, for example, an integrated optical phase modulator PM_n or, as illustrated in figure 6, a piezoelectric phase modulator PM_n . The fiber polarizers 8_n , which are

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part of the means 6, 7 for guiding light, are not followed by a turned splice, but by a simple, non-rotated splice, which is therefore not illustrated. The first means 6 and second means 7 include fiber couplers 18_n. The feeder fiber 10_n of the sensor head H_n is directly connected optically to one of the output ends, on the sensor head side, of the coupler 18_n. The other output end, on the sensor head side, of the coupler 18_n is optically connected to the phase modulation unit PME_n or the phase modulator PM_n, respectively. The phase modulation unit PME_n is optically connected, in turn, to the feeder fiber 10_n' of the sensor head H_n. It holds advantageously for a spacing δ of the phase modulator PM_n of the coupler 18_n that $\Delta n_{gr} \cdot \delta$ is smaller than the coherence length of the light of the light source 1, Δn_{gr} being the difference between the group refractive indices for the two mutually orthogonal light modes.

In the case of such a sensor with Sagnac configuration, lightwaves propagating in opposite directions and polarized parallel to one another are phase-modulated by each of the N phase modulators PM_n.

Figure 7 shows a further advantageous embodiment of the invention. This sensor resembles the sensor illustrated in figure 5 and is described starting therefrom. Instead of a detector 2, the sensor in accordance with figure 7 has N = 3 detectors 2_n. These are arranged in each case on an arm, averted from the respective sensor head H_n, of the couplers 14, 17 and 3₃. Each detector 2_n is connected via a detector signal line D_n to the control and evaluation unit 5. Each of the three detectors 2_n serves for detecting the signals originating from the respective sensor head H_n. The corresponding lightwaves therefore pass fewer couplers by comparison with a design in accordance with figure 5. Consequently, less loss in intensity occurs, and higher optical powers can be detected. This leads

to a better signal-to-noise ratio. Again, the other embodiments discussed can also be provided in a similar way with N detectors 2_n .

5 In order to achieve a virtually perfect reciprocity, and thus stability of the sensors when taking measurements, the detectors 2_n are arranged on the said couplers. The detectors 2_1 and 2_2 are arranged in figure 7 at a reciprocal output, not so, however, the
10 detector 2_3 . An alternative design (not illustrated) in which more light power can be detected results when, by analogy with the detector 2_3 , each of the detectors 2_n is arranged at the respective coupler 3_n , each of the detectors 2_n then being arranged at a non-reciprocal
15 output.

In the case of the modulation circuits PME, PME_n , the means for changing the direction of polarization 9 can be arranged without any, with one or with several phase
20 modulators PM, PM_n in the same fiber branch. When several phase modulators are arranged in one modulation circuit, these can be distributed alternately over the two fiber branches. It is also possible in a modulator circuit for two or more phase modulators operated with
25 the same frequency ν_n to replace a single phase modulator operated with this frequency ν_n . These phase modulators can be arranged in the same or in different fiber branches of the modulator circuit.

30 Instead of only one phase modulator PM_n , it could also be possible for several phase modulators PM_n per sensor head H_n to be arranged in a design with Sagnac configuration such as in figure 6, for example. An arrangement at the same or different ends of the
35 respective sensor coil 12_n would be possible.

In principle, in the exemplary embodiments discussed the divider ratios of the couplers are advantageously

selected in such a way that substantially the same light intensity is coupled into each sensor head H_n .

In principle, in the exemplary embodiments discussed
5 the number and arrangement of the couplers is advantageously selected in such a way that the reciprocity obtains for all light paths. This means that no non-reciprocal phase shifts occur owing to the design of the sensor, but only the non-reciprocal
10 Faraday phase shift $\Delta\phi_n$ to be detected, and the quasi static phase shift, caused by the phase modulation, for the effective shifting of the operating point during detection and evaluation. For example, the design in accordance with figure 1 would no longer be reciprocal,
15 and thus vulnerable to disturbing influences (mechanical, thermal), were the two couplers 14 and 3 to be replaced by a single coupler.

It is also possible in principle to make use instead of
20 two serially connected couplers of a single coupler that couples one or two light paths into more than two light paths. For example, in figure 1 the couplers 4 and 15 would correspondingly be replaced by a 2x3 coupler, which has two inputs and three outputs, in
25 which case one sensor head H_n would be coupled to each of the three outputs via one optical supply lead 10_n each. However, this entails an adequate maintenance of the polarization of the coupler.

30 Of course, various types of the phase modulation units PME described and the phase modulators PM can be combined in a sensor. Moreover, it is also possible to conceive of phase modulators that differ from piezoelectric and integrated optical phase modulators.

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It is advantageous of the sensors described that they require only a single control and evaluation unit 5, and only a single signal processor. It is further

advantageous that only a single light source 1 is required. It is further advantageous that it is possible to manage with only a single detector 2. All of these advantages result in a simple and cost effective design of the sensor.

Sensors according to the invention can be used to measure N currents or N magnetic fields. It is also possible to use some of the sensor heads H_n redundantly. For example, in the case of $N = 6$ sensor heads H_n , it is advantageously possible for two sensor heads in each case to measure the same current of a phase of an electric high voltage system. One of the two sensor heads advantageously has more turns of the sensor coil, and serves the purpose of exact current measurement, for example for power billing, while the other sensor head with fewer turns has a larger measuring range and is used for the purpose of power system protection, it being possible to use it to measure overcurrents unambiguously in the case of a short circuit.

Two further methods are described below, and these can be used to achieve a good signal-to-noise ratio with the aid of only one phase modulator PM and only one modulation frequency ν in a time division multiplexing method by virtue of the fact that the amplitude $\alpha_{0,n}$ of the differential phase can be set optimally for each of the N sensor heads (compare the designs of figures 1 and 3):

This can be achieved by a suitable selection of the differences between the various overall optical circulation lengths Λ_n from the light source through the n th sensor head to the detector. The amplitude $\alpha_{0,n}$ of the nearest sensor head (smallest Λ_n), for example, is selected optimally by appropriate selection of the overall circulation length Λ_n . This means that this is

$\alpha_{0,n} = 1.84$ in the case of detection at the first and second harmonics. The equation already mentioned

$$\alpha_{0,n} = 2 \cdot \phi_{0,n} \cdot \sin(2\pi v T_n / 2)$$

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can now be used to select the segment increment relating to the next longest total optical circulation length Λ_n such that the argument of the sine term changes by π :

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$$2\pi v_n \Delta T / 2 = 2\pi v \Delta \Lambda / c = \pi$$

and thus

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$$\Delta \Lambda = c / 2v,$$

$\Delta \Lambda$ being the segment increment by which the minimum total optical circulation length Λ_n must be extended in order to achieve the change by π , and ΔT being the corresponding minimum extension of the circulation time of the light. If the further total optical circulation lengths Λ_n are increased by a multiple of $\Delta \Lambda$ by comparison with the smallest Λ_n , the detection is possible for all sensor heads having an optimum signal-to-noise ratio. $\Delta \Lambda = 796$ m for a modulation frequency of 130 kHz. The higher the modulation frequency v is selected, the smaller is the required fiber length.

The second possibility of setting the amplitude $\alpha_{0,n}$ to its optimum value (for example 1.84) by using only one phase modulator PM and only one modulation frequency v in the time division multiplexing method for all the sensor heads H_n consists in making a suitable selection of the amplitude of the phase modulation $\phi_{0,n}$ in appropriate time windows by means of a suitable selection of the driver voltage of the phase modulator PM. Thus (compare figure 2), when a signal originating from the first sensor head H_1 is detected starting from

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the time $\Delta\tau_1$ after the beginning of a light pulse from the light source 1, the amplitude $\phi_{0,1}$ of the phase modulation is selected in such a way that $\alpha_{0,1}$ is optimum. When a signal originating from the second
5 sensor head H_2 is detected starting from the time $\Delta\tau_2$ after the beginning of a light pulse from the light source 1, the amplitude $\phi_{0,2}$ of the phase modulation is to be selected in such a way that $\alpha_{0,2}$ is optimum, in which case $\alpha_{0,1}$ and $\alpha_{0,2}$ and the corresponding driver
10 voltages and $\phi_{0,1}$ and $\phi_{0,2}$ are generally of different magnitude. Note that in the case of low modulation frequencies ν the time required to change the amplitudes $\phi_{0,n}$ of the phase modulation can be substantially longer than the repetition frequency of
15 the light pulse $1/\Delta t$. The gaining of signals is interrupted during this dead time in which the amplitude is changed, and so a worsened signal-to-noise ratio results.

List of reference symbols

	1	light source
	2, 2 _n	detector, photodiode
5	3, 3 _n	end, on the detector side, of the phase modulation unit; fiber coupler
	4, 4 _n	end, on the sensor head side, of the phase modulation unit; fiber coupler
	5	control and evaluation unit: signal processor
10	6	first means (for guiding light of the light source into an end, on the detector side, of the phase modulation unit)
	7	second means (for guiding light from the end, on the detector side, of the phase modulation unit to the detector)
15	8, 8 _n	polarizer, fiber polarizer
	8', 8' _n	polarizer, fiber polarizer
	9, 9 _n	means for changing the direction of polarization, 90°splice
20	9', 9' _n	means for changing the direction of polarization, 45°splice
	10 _n	fiberoptic supply lead
	11 _n , 11' _n	phase delay element, $\lambda/4$ element
	12 _n	sensor coil, magnetooptically active fiber
25	13 _n	mirror, mirrored end
	14	fiber coupler
	15	fiber coupler
	16	fiber coupler
	17	fiber coupler
30	18 _n	fiber coupler
	C _n	current conductor
	D, D _n	detector signal line
	H _n	sensor head
35	_{e1,n}	electric current to be measured
	ℓ_n	modulation-relevant optical path length
	L	light control signal line
	M, M _n	modulator signal line

	N	whole number with $N \geq 2$; number of sensor heads
	Δn_{gr}	difference between the group refractive indices for the two mutually orthogonal light modes
5	p	positive whole number
	PM, PM_N	phase modulator, piezoelectric modulator, integrated optical modulator
	PME, PME_n	phase modulation unit, modulator circuit
10	q	positive whole number
	S_n	output signal
	T_n	modulation-relevant circulation time
	Δt	light pulse spacing
	V	Verdet constant (of a sensor coil)
15	$\alpha_{o,n}$	amplitude of the modulation of the differential phase
	δ	spacing (of the phase modulator from the coupler in the Sagnac configuration)
20	$\Delta\phi_n$	differential phase shift on the basis of the Faraday effect
	Λ_n	total optical circulation length (from the light source 1 through the nth sensor head to the nth detector)
25	ν_n	modulation frequency
	$\phi_{o,n}$	amplitude of the phase modulation
	τ	pulse duration (of a light pulse in the case of time division multiplexing)
	$\Delta\tau_n$	transit time of a light pulse from the light source to the detector
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